

Th-3 DIGITAL SIGNAL PROCESSING

Full Marks: 80

Time- 3 Hrs

Answer any five Questions including Q No.1& 2

Figures in the right hand margin indicates marks

1. Answer **All** questions 2 x 10
 - a. State Sampling Theorem.
 - b. Draw the following type of signals. (i) Continuous aperiodic signal (ii) Discrete periodic signal
 - c. Define a causal signal and causal system.
 - d. Draw a discrete time unit step signal and ramp signal and represent them mathematically.
 - e. Determine z-transform of signal $y(n) = 3^n u(n)$.
 - f. An input signal $x(n)$ is applied to a LTI system having impulse response $h(n)$, then write the expression for the output of the system.
 - g. Find the inverse z-transform of $X(Z) = \left(\frac{Z}{Z-2}\right)$ (ROC: $|Z| > 2$).
 - h. Define ROC.
 - i. List any two types of digital filters.
 - j. State any two applications of FFT algorithm.

2. Answer **Any Six** Questions 6 x 5
 - a. Explain different steps of analog to digital signal conversion process.
 - b. A causal LTI system is described by the difference equation
$$y(n) - \frac{3}{4}y(n-1) + \frac{1}{8}y(n-2) = 2x(n)$$
Determine impulse response, $h(n)$ of the system.
 - c. Write down the advantages of Digital Signal Processing over analog signal processing.
 - d. State and explain any five properties of DFT.
 - e. Let $x(n) = \delta(n) + 3\delta(n-1) - 2\delta(n-3)$ and $h(n) = 2\delta(n+1) + \delta(n) - 4\delta(n-1)$. Compute and plot $y(n) = x(n) * h(n)$
 - f. Find 4-point DFT of $x(n) = \{1, 0, 1, 0\}$
 - g. Find energy (E) and average power (P) of $x(n) = \left(\frac{1}{2}\right)^n u(n)$.

3. With a neat block diagram explain different parts of digital to analog converter. 10

- 4 (i) Define LTI system. [1] 10
- (ii) Determine whether the following systems are linear time invariant.[9]
- (a) $y(n) = nx(n-4)$ (b) $y(n) = e^{x(n)}$ (c) $y(n) = x(n) - x(n-1)$
- 5 Consider the z – transform $X(Z) = \frac{3 - \frac{5}{6}Z^{-1}}{(1 - \frac{1}{4}Z^{-1})(1 - \frac{1}{3}Z^{-1})}$ with $ROC: \frac{1}{4} < |x| < \frac{1}{3}$. 10
- Determine its inverse z – transform.
- 6 (i) Differentiate between FIR and IIR filters. [5] 10
- (ii) Determine circular convolution of the following sequences. [5]
- $g(n) = \{1, 2, 0, 1\}$ and $h(n) = \{2, 2, 1, 1\}$
- \uparrow
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- 7 Determine 8-point DFT of a sequence $x(n) = \{1, 2, 3, 0, 2, 1, 0, 4\}$ using radix –2 DIT FFT algorithm. 10